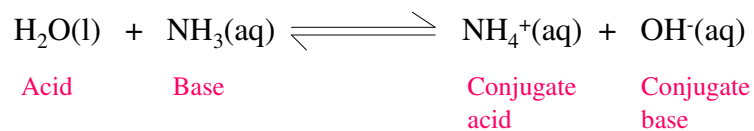
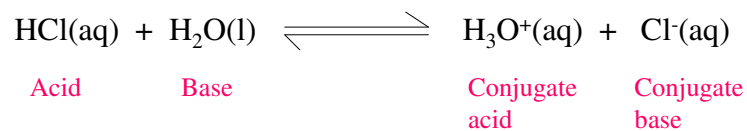


# pH calculations

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## Brønsted-Lowry concept of acids and bases

- Acid is a proton donor
- Base is a proton acceptor



## Which of the following are conjugate acid-base pairs?

A) HCl, NaOH

**B) H<sub>2</sub>O, OH<sup>-</sup>**

C) H<sub>2</sub>SO<sub>4</sub>, SO<sub>4</sub><sup>2-</sup>

**D) H<sub>2</sub>SO<sub>3</sub>, HSO<sub>3</sub><sup>-</sup>**

E) HClO<sub>4</sub>, ClO<sub>3</sub><sup>-</sup>

**F) H<sub>3</sub>C-NH<sub>2</sub>, H<sub>3</sub>C-NH<sub>3</sub><sup>+</sup>**

## Autoionization of water

Water is amphoteric as it can behave both as acid and base



Ion-product constant for water:

$$K_w = [\text{H}_3\text{O}^+][\text{OH}^-] = [\text{H}^+][\text{OH}^-]$$

In pure water at 25 °C:

$$[\text{H}^+] = [\text{OH}^-] = 1.0 \times 10^{-7} \text{ mol/L}$$

$$K_w = (1.0 \times 10^{-7} \text{ mol/L}) \times (1.0 \times 10^{-7} \text{ mol/L}) = \mathbf{1.0 \times 10^{-14} \text{ mol}^2/\text{L}^2}$$

Constant!

# pH

$$\text{pH} = -\log_{10}(\text{activity of H}^+)$$

$$\text{pOH} = -\log_{10}(\text{activity of OH}^-)$$

Ion-product of water (constant!):

$$\text{pH} + \text{pOH} = 14$$

Activity =  $f \cdot c$   
 $f$  is activity coefficient,  
 $f < 1$ ,  
 $c$  is molar concentration

E.g.:

$$\text{pH}=7 \text{ (neutral): } [\text{H}^+] = 10^{-7} \text{ M} = 0.0000001 \text{ mol/l}$$

$$\text{pH}=1 \text{ (acidic): } [\text{H}^+] = 10^{-1} \text{ M} = 0.1 \text{ mol/l}$$

$$\text{pH}=13 \text{ (alkaline): } [\text{H}^+] = 10^{-13} \text{ M} = 0.0000000000001 \text{ mol/l}$$

## Strong acid

E.g. HCl, HNO<sub>3</sub>, H<sub>2</sub>SO<sub>4</sub>

In aqueous solution fully dissociates to H<sup>+</sup> and A<sup>-</sup>

pH of strong acid can be calculated as

$$\text{pH} = -\log (f \times [\text{H}^+])$$

For HCl:  $[\text{H}^+] = [\text{HCl}]$

For H<sub>2</sub>SO<sub>4</sub>:  $[\text{H}^+] = 2 \times [\text{H}_2\text{SO}_4]$

### **Calculating the pH of strong acid solutions**

Example: Calculate the pH of 0.06 mol/L HCl.

$$\text{pH} = -\log 0.06 = \underline{\underline{1.22}}$$

### **Calculating the pH of strong acid solutions**

Example 2: Calculate the pH of 0.02 mol/L H<sub>2</sub>SO<sub>4</sub>.

$$\text{pH} = -\log 0.04 = 1.3979 = \underline{\underline{\sim 1.4}}$$

## Calculating the pH of strong acid solutions

Example 3: Calculate the pH of  $1.0 \times 10^{-10}$  M HCl.

$$\text{pH} = -\log(10^{-10}) = 9 \quad \dots \text{alkaline?}$$

Water contributes more protons than HCl in this case ( $10^{-7}$  M),  
pH will be the same as in pure water, i.e. 7

## Strong base

E.g. NaOH, KOH,  $\text{Ba}(\text{OH})_2$

In aqueous solution fully dissociate to metal ion and  $\text{OH}^-$

pH of strong base can be calculated as

$$\text{pOH} = -\log(f \times [\text{OH}^-])$$

$$\text{pH} = 14 - \text{pOH} = 14 - (-\log(f \times [\text{OH}^-]))$$

For NaOH:  $[\text{OH}^-] = [\text{NaOH}]$

For  $\text{Ba}(\text{OH})_2$ :  $[\text{OH}^-] = 2 \times [\text{Ba}(\text{OH})_2]$

## Calculating the pH of strong base solutions

Example:

a) Calculate the pH of NaOH 0.5 mol/L.

$$\text{pH} = 14 - (-\log 0.5) = \underline{\sim 13.7}$$

b) If this solution is diluted 10-fold, what will be the resulting pH?

$$\text{pH} = \underline{\sim 12.7}$$

## Weak acid

E.g.  $\text{H}_2\text{CO}_3$ ,  $\text{CH}_3\text{COOH}$

Only some small fraction of molecules in solution dissociates to anion and proton:



$$K_d = \frac{[\text{CH}_3\text{COO}^-] \times [\text{H}^+]}{[\text{CH}_3\text{COOH}]}$$

$$\text{pH} = \frac{1}{2} \times \text{pK} - \frac{1}{2} \times \log [\text{AH}]$$

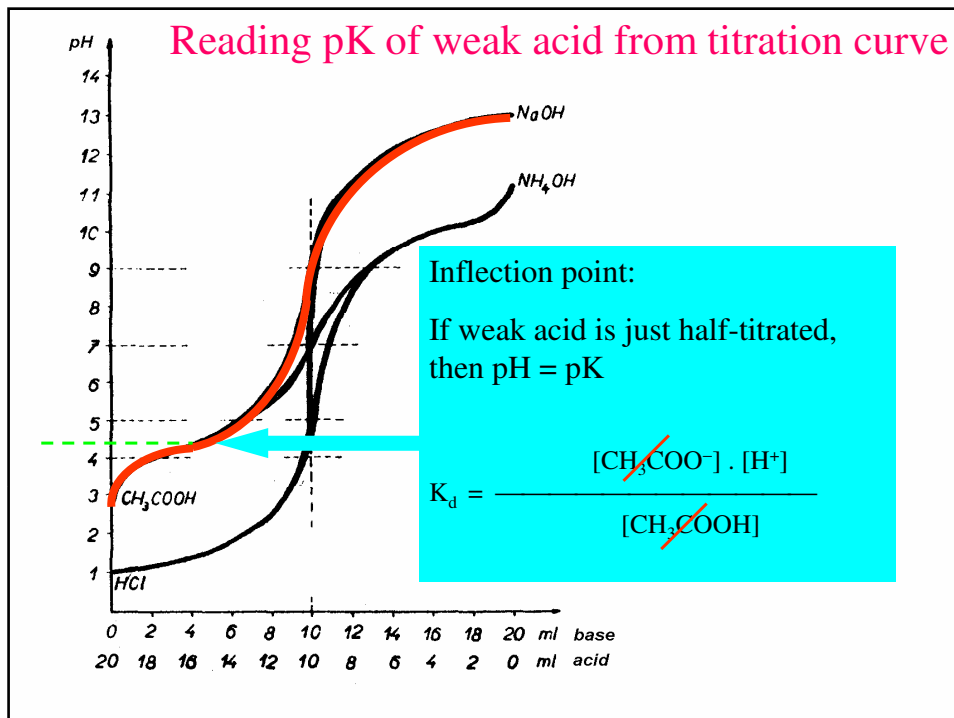
$$\text{pK} = -\log K_d$$

- If we know pK ( $K_d$ ) and concentration of a weak acid solution, we can calculate (predict) pH of the solution:

$$\text{pH} = \frac{1}{2} \times \text{pK} - \frac{1}{2} \times \log [\text{AH}]$$

- If we measure pH of a weak acid solution of a known concentration, we can determine its pK ( $K_d$ ):

$$\text{pK} = 2 \times \text{pH} + \log [\text{AH}]$$



## Calculating the pH of weak acid solutions

Example: Calculate the pH of 0.01 mol/L acetic acid.

$$K_a = 1.8 \times 10^{-5}.$$

$$\text{pH} = \frac{1}{2} \times \text{pK} - \frac{1}{2} \times \log [\text{AH}]$$

$$\text{pK} = -\log(1.8 \times 10^{-5}) = 4.7447$$

$$\begin{aligned} \text{pH} &= \frac{1}{2} \times 4.7447 - \frac{1}{2} \times \log 0.01 = \\ &= 2.372 - (-1) = \underline{3.372} \end{aligned}$$

## Calculating the pH of weak acid solutions

Example 2: Calculate the pH of 0.1 mol/L hypochlorous acid.

$$K_a = 3.5 \times 10^{-8}.$$

$$\text{pH} = \frac{1}{2} \times \text{pK} - \frac{1}{2} \times \log [\text{AH}]$$

$$\text{pK} = -\log(3.5 \times 10^{-8}) = 7.456$$

$$\begin{aligned} \text{pH} &= \frac{1}{2} \times 7.456 - \frac{1}{2} \times \log 0.1 = \\ &= 3.728 - (-0.5) = \underline{4.228} \end{aligned}$$



## Weak base

E.g.  $\text{NH}_3(\text{aq})$ , organic amines

A fraction of molecules in aqueous solution accepts proton from water:



$$K_d = \frac{[\text{NH}_4^+] \times [\text{OH}^-]}{[\text{NH}_3]}$$

$$\text{pOH} = \frac{1}{2} \times \text{pK} - \frac{1}{2} \times \log [\text{B}]$$

$$\text{pH} = 14 - \text{pOH} = 14 - \frac{1}{2} \times \text{pK} + \frac{1}{2} \times \log [\text{B}]$$

## Calculating the pH of weak base solutions

Example: Calculate the pH of 5 mol/L aqueous ammonia.

$$K_b = 1.8 \times 10^{-5}$$

$$\text{pH} = 14 - \frac{1}{2} \times \text{pK}_b + \frac{1}{2} \times \log [\text{B}]$$

$$\text{pK}_b = -\log(1.8 \times 10^{-5}) = 4.745$$

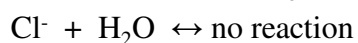
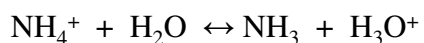
$$\begin{aligned} \text{pH} &= 14 - \frac{1}{2} \times 4.7447 + \frac{1}{2} \times \log 5 = \\ &= 14 - 2.37236 + 0.349 = \underline{11.977} \end{aligned}$$

## Hydrolysis of salts

Reaction of dissolved salts with water, e.g.:

A) Anion from a strong acid, cation from a weak base, e.g.

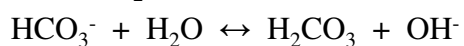
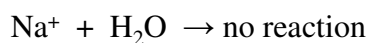
$\text{NH}_4\text{Cl}$ :



...pH is acidic

B) Anion from a weak acid, cation from a strong base, e.g.

$\text{NaHCO}_3$ :



...pH is alkaline

Calculate the pH of 0.5 mol/L sodium hydrogen carbonate,  $\text{NaHCO}_3$ .

The  $K_{a1}$  of carbonic acid is  $4.3 \times 10^{-7}$ .

$$\text{pH} = 14 - \frac{1}{2} \times \text{p}K_b + \frac{1}{2} \times \log [\text{B}]$$

$$\text{p}K_a = -\log(4.3 \times 10^{-7}) = 5.3665$$

$$\text{p}K_b = 14 - 5.3665 = 8.6335$$

$$\begin{aligned} \text{pH} &= 14 - \frac{1}{2} \times 8.6335 + \frac{1}{2} \times \log 0.5 = \\ &= 14 - 4.31675 + (-0.30103) = \underline{9.382} \end{aligned}$$